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Massachusetts Institute of Technology

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**AN INVESTIGATION INTO THE GROWTH
OF A BOILING BOUNDARY LAYER
IN TURBULENT FLOW**

John Calvin Dyer

AN INVESTIGATION INTO THE GROWTH
OF A BOILING BOUNDARY LAYER IN
TURBULENT FLOW

by

John Calvin Dyer

B.S., United States Naval Academy
(1947)

SUBMITTED IN PARTIAL FULFILLMENT

OF THE REQUIREMENTS FOR THE

DEGREE OF MASTER OF SCIENCE

IN NUCLEAR ENGINEERING

at the

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

July 1956

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AN INVESTIGATION INTO THE GROWTH
OF A BOILING BOUNDARY LAYER IN
TURBULENT FLOW

by

Lieutenant John Calvin Dyer, U.S.N.

Submitted to the Department of Chemical Engineering
on 20 August 1956 in partial fulfillment of the requirements
for the degree of Master of Science in Nuclear Engineering.

ABSTRACT

The thickness of the boiling, bubble, boundary layer in forced convection flow in rectangular geometry was measured by photographs. The test section had a rectangular cross section (1/2 inch x 1/4 inch) which consisted of two opposite, electrically heated, stainless steel walls and two glass walls. The ratio of heated strip length to the spacing between the strips was about sixty. The range of the variables investigated was: heat flux density 0 to 475,000 Btu/hr ft²; test section flow velocity 0 to 5 ft/sec; pressure 0 to 56 psia, and liquid subcooling between 27°F and 108°F at the test section inlet.

The bubble boundary layer thickness was plotted against a parameter which expressed the calculated bulk subcooling of the liquid at the point where the bubble layer thickness was measured. The plots show quantitatively the behavior of the bubble layer under various conditions of subcooling, flow, and heat flux density. An attempt was made to include the conditions of nucleation of boiling as a unifying parameter for the layer growth. While a significant relationship was indicated, there is little experimental basis for the proper value of nucleation superheat necessary at the pressures investigated. In addition there are undoubtedly other nucleation variables which are significant. A generalized correlation of bubble layer growth was not achieved.

Thesis Supervisor: John A. Clark

Title: Assistant Professor of Mechanical Engineering

Submitted to the Department of Chemical Engineering
on 10 March 1950 in partial fulfillment of the requirements
for the degree of Master of Science in Chemical Engineering.

ABSTRACT

The behavior of the boiling, bubble, boundary layer
in forced convection flow in pipes, ducts, vessels, etc.
was investigated. The test section had a rectangular
cross section (1/2 inch x 1/2 inch) which consisted of two
opposite, electrically heated, stainless steel walls and
two glass walls. The walls of heated walls were 1/2 inch
apart. The test section was about 1/2 inch. The range of
the variables investigated was: heat flux density 0 to
100,000 Btu/hr-ft²; inlet velocity 0 to 10 ft/sec;
inlet pressure 0 to 20 psia; and liquid subcooling between
100°F and 1000°F at the test section inlet.
The bubble boundary layer thickness was plotted against
a parameter which represented the calculated bulk subcooling
at the inlet of the pipe where the bubble layer fol-
lowed. The data show qualitatively the
behavior of the bubble layer under various conditions of
subcooling, flow, and heat flux density. An attempt was
made to include the conditions of nucleation of bubble
in a unified parameter for the layer growth. While a
slight relationship was indicated, there is little
experimental basis for the proper value of subcooling
required for the bubble growth. The parameter investigated, the
subcooling, is not necessarily the most important variation
which may influence. A generalized correlation of
bubble layer growth was not achieved.

These measurements were made at

Massachusetts Institute of Technology, Cambridge, Massachusetts

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He is grateful to the U.S. Naval Postgraduate School, Monterey, California for the necessary financial assistance.

He wishes to thank the craftsmen, particularly Robert Simpson, Herbert Norquist and William Liddy of the Central Tool Shop of the Boston Naval Shipyard for manufacturing the test section. Much credit is also given to Fred Johnson and Edward Hartell of the Heat Transfer Laboratory at the Massachusetts Institute of Technology for their ready assistance in the myriad details of assembling the test loop. In addition, the success of the photographic work was due to the skill and patience of Fred Johnson.

He also wishes to thank his wife, Glenys Dyer, who typed this thesis.

Finally, the author wishes to express his appreciation to the many friends and colleagues who have helped him in the past and who are helping him now. In particular, he wishes to thank the many friends who have helped him in the past and who are helping him now.

The author wishes to express his appreciation to the many friends and colleagues who have helped him in the past and who are helping him now.

The subject of this report is Professor John A. Clark, for
 engineering and engineering education and in the
 Department of Mechanical Engineering of the Massachusetts
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 the test section. Such credit is also given to Fred
 Johnson and Robert Hurrell of the Heat Transfer Laboratory
 at the Massachusetts Institute of Technology for their years
 assistance in the design details of assembling the test loop.
 In addition, the success of the program is due to
 to the skill and guidance of Fred Johnson.
 He also wishes to thank his wife, Nancy Clark, and
 typed this thesis.

INTRODUCTION

The use of flat plate type fuel elements in nuclear reactors and the desire to achieve the higher heat transfer rates that are possible with the boiling process require more fundamental information on boiling under conditions of flat plate geometry. It was the objective of this investigation to make a photographic study of the boiling boundary layer growth under flow conditions using geometry and a ratio of coolant volume to heating surfaces which would more nearly approximate conditions in a nuclear reactor core. Previous investigations of pool boiling have generally used single heated wires or rods in a pool of water where the bubble size was large in relation to the heating surfaces, and the volume of fluid was much greater than the heating surface. The forced convection boiling has been done predominantly inside circular channels which is not the geometry of interest here.

Apparently the first work with rectangular flow channels was done by Gunther (1)* who had the heating strip in the center of the channel with water on both sides. As the intention was a study of bubble dynamics, rather than the growth of a bubble layer, the heated strips used by Gunther were not long. Argonne National

* Numbers in parentheses refer to the references in the bibliography.

INTRODUCTION

The use of first class type metal elements in printing

has been the desire to achieve the highest possible quality

of the printed matter and the uniformity of the printed

matter. The investigation of the boiling process in printing

of first class quality. It was the objective of this

investigation to make a quantitative study of the boiling

process under these conditions and to determine the

and a ratio of certain values to boiling surface which

would not usually approximate conditions in a printer

printer case. Previous investigations of boiling

have generally used single heated plates or tubes in a

pool of water where the bubble size was large in relation

to the heating surface, and the volume of fluid was much

greater than the heating surface. The forced convection

boiling has been done experimentally inside of tubes

channels which is not the geometry of interest here.

Apparently the first work with rectangular flow

channels was done by Gifford (1)* who had the heating

strip in the center of the channel with water on both

sides. In the investigation was a study of bubble expansion,

rather than the growth of a bubble layer, the reason

being that by Gifford's work was not done. Previous workers

* Numbers in parentheses refer to the references in the bibliography.

Laboratory has done extensive work with flat plate geometry in boiling conditions, but the only published information to date has been for natural convection (2). The writer was informed that work on boiling in forced convection in rectangular flow channels had been done at A.L., but no reports were available.

None of the foregoing published investigations used forced convection in flow geometry with oppositely facing heating elements having a large L/y , ratio of length to spacing between plates. The heat transfer section which was used consisted of two electrically heated flat, stainless steel (18-8) strips with degassed (de-aerated) distilled water flowing between them. L/y for this experiment was about 60. The range of the variables investigated was: heat flux density 0 to 475,000 Btu/hr ft²; test section flow velocity 0 to 5 ft/sec; pressure at test section outlet 0 to 56 psia, and liquid subcooling between 27°F and 108°F at the test section inlet.

A description of the apparatus used, a discussion of the test procedure, and the test results are given in subsequent sections.

DESCRIPTION OF APPARATUS

The experimental equipment used to carry out this investigation is shown in the accompanying diagrams.

Fig. 1 is a schematic flow diagram of the test loop.

Fig. 2 is a photograph of the apparatus showing the test section in the vertical position. The pump and electrical preheaters are not visible in the photograph.

Distilled and degassed water was circulated in the test loop. This water was preheated before entering the test section by two electric heaters (electric Chromalox immersion heaters, type HT 270, 7000 watts, 240 volts, E.I. Wiegand Co., Pittsburgh, Pa.). These heaters were controlled by Variacs, type V1CG2, General Radio Co., Cambridge, Mass. A single coiled tube heat exchanger using cold water was used to cool the water leaving the test section before entering the pump (Westinghouse totally enclosed centrifugal pump, model 30A, 220 volts, 3 phase, 60 cycle). This pump required an oil cooling system which had an oil to water cooled heat exchanger (Ross Heater and Manufacturing Co., Buffalo, N.Y.) and an electrically driven centrifugal pump, 10 gpm, Allis Chalmers Manufacturing Co., Kenwood, Ohio. The motor for the oil pump was 3/4 HP, 440 volt, 60 cycle, 3 phase, General Electric. The water circulating pump discharged to a 3/4 inch square edged orifice for flow

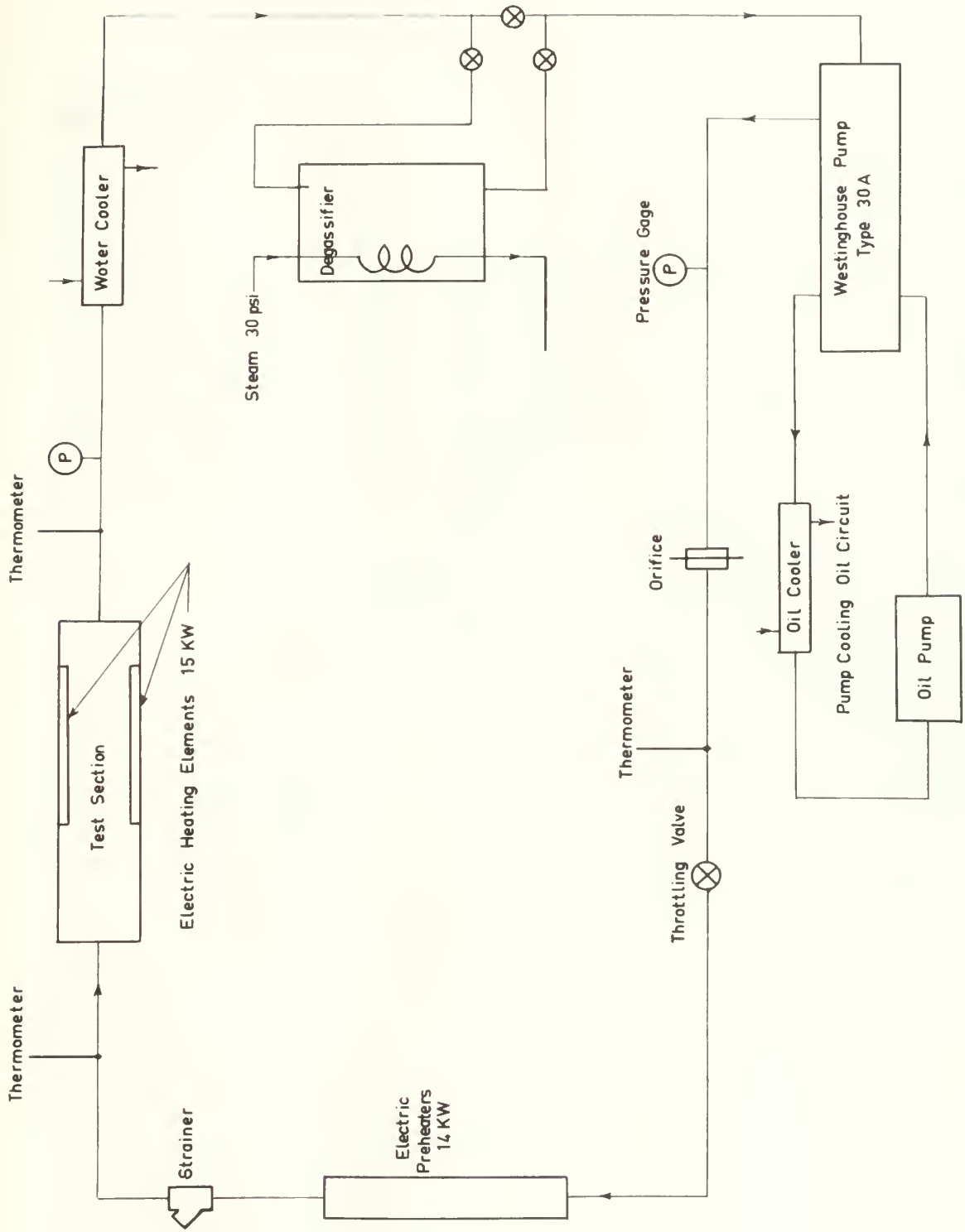


Fig. 1 - SCHEMATIC FLOW DIAGRAM

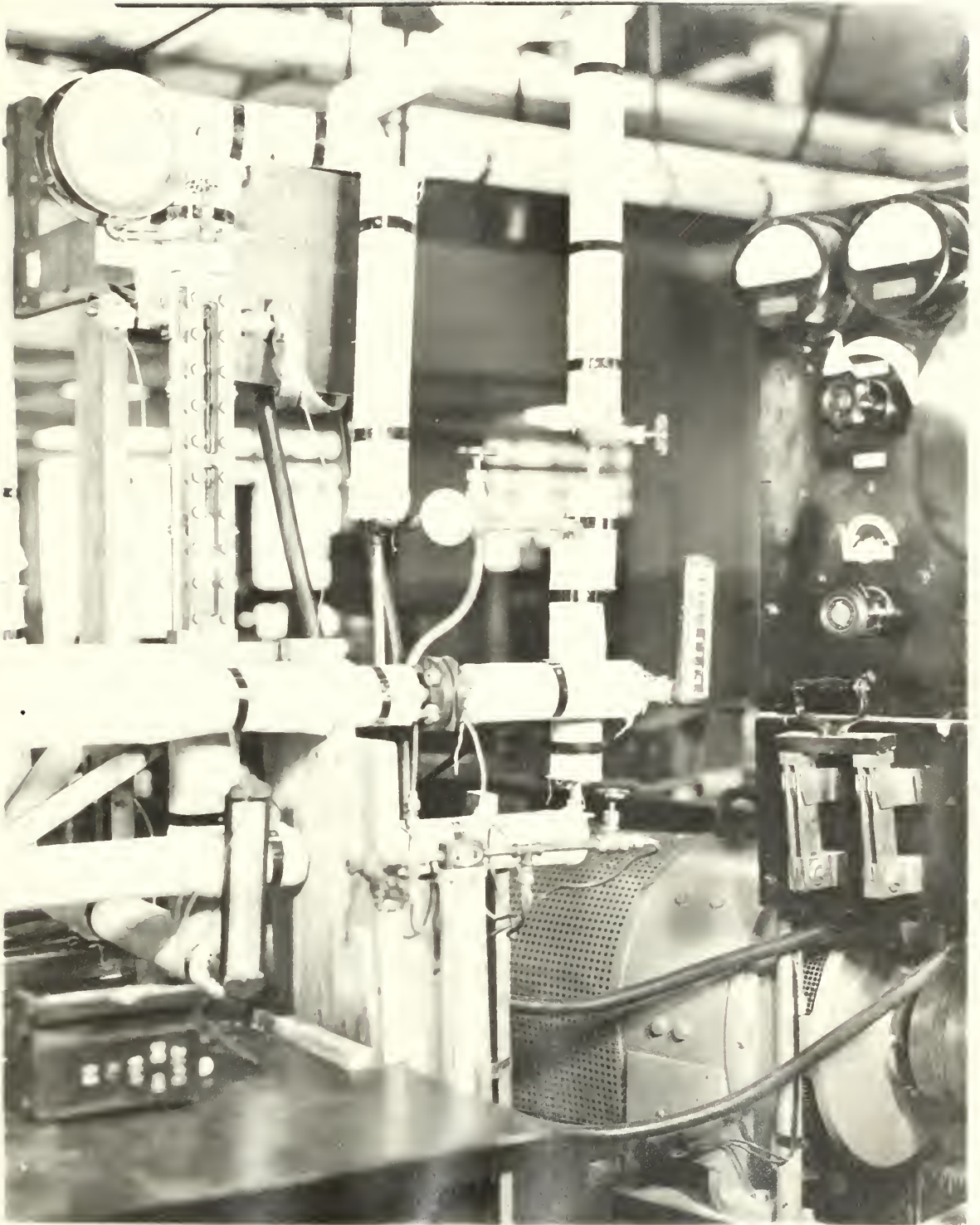


Fig. 2 - Photograph of Apparatus

measurements. The manometer used was a Merriam 20 inch U-manometer, type B-1103. The flow rate was controlled by a valve on the discharge side of the pump.

The test section consisted essentially of a rectangular flow channel, $1/4$ inch x $1/2$ inch cross section, with electrically heated stainless steel (18-8) strips forming two of the opposite walls. The other two walls were glass which permitted viewing the nucleate boiling bubble formation on the heated strips. The heated strips were 15.0 inches in length, giving an L/y of approximately 60. The inlet approach section was also rectangular, $1/4$ inch x $3/8$ inch cross section and an L/y of 50. The inlet and outlet sections (Fig. 3) were necessarily narrower, i.e. $3/8$ inch instead of $1/2$ inch to provide end support for the glasses. Tapered transitions were made at these points. The test section outlet had the same cross sectional dimensions as the inlet but was much shorter, about $3\ 1/2$ inches.

The main part of the test section was mild steel (Fig. 4). This provided a frame to receive the water inlet and outlet sections, the electrical conductors and heating strips, and the glass windows (Jerguson gage glasses, series 5, 17 inch length) which were clamped by modified Jerguson gage glass covers, series 5. Electrical insulation between the stainless steel heating strips and the mild steel frame was achieved by using

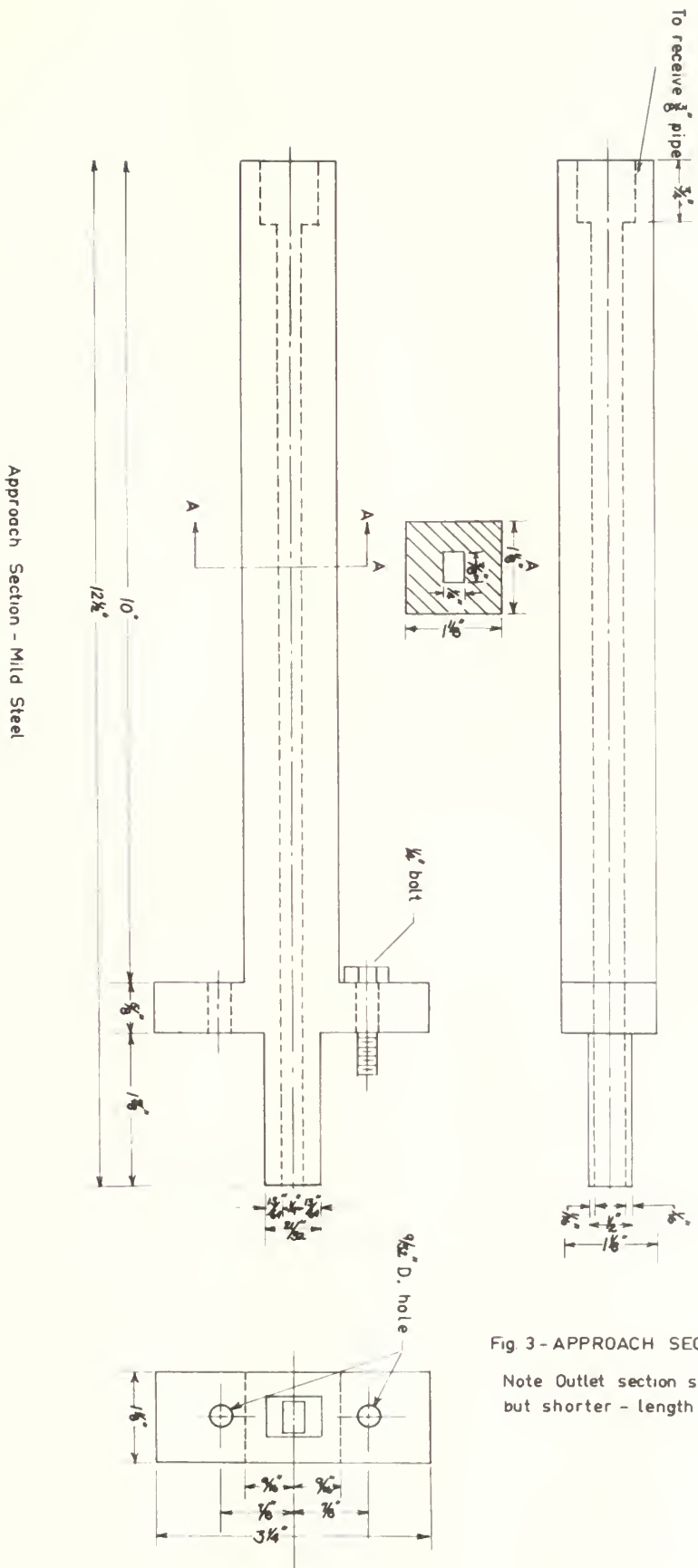


Fig 3 - APPROACH SECTION

Note Outlet section similar, but shorter - length $3\frac{1}{2}"$

TEST SECTION BODY - mild steel

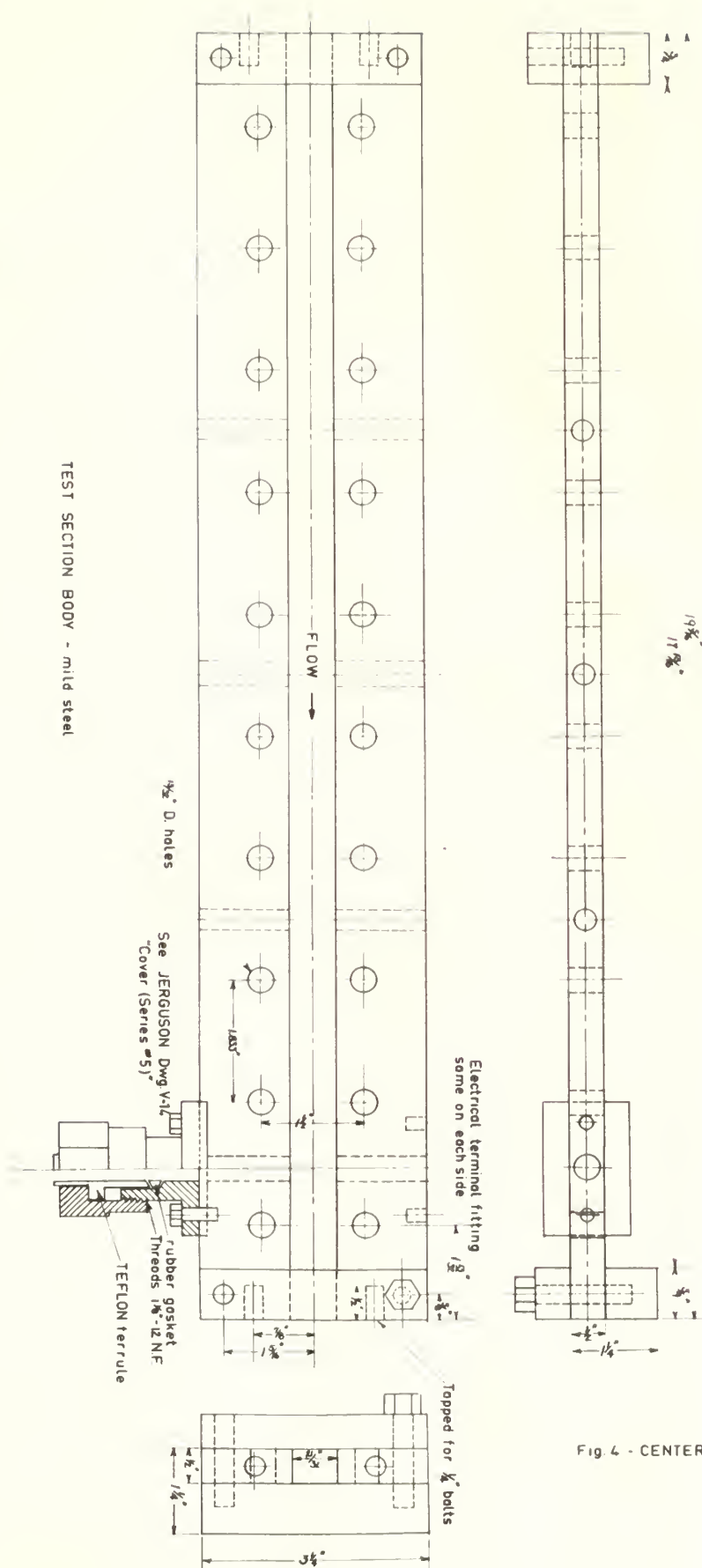


Fig. 4 - CENTER SECTION

DuPont Teflon plastic. The heater strips were electrically connected in series by a copper bus or connection piece located at the water inlet end of the heater strips (piece "2", Fig. 5). This electrical arrangement was chosen because of the generator characteristics used to provide the electrical power. The power for the heating strips came from a motor-generator set (motor manufacturer, L.J. Land and Co., 220 volts, 60 cycle, 3 phase, 65 amps, 1150 rpm; generator manufacturer, General Electric Corp., model 53A532, 15 volts, 1000 amps).

The distilled water was degassed by boiling in a stainless steel drum heated by a submerged steam coil using 30 pounds saturated steam. Water was transferred to and from this drum, which also served as a system reservoir, by the Westinghouse pump.

Difficulty was experienced with very small rust particles, apparently from the steel jacketed preheaters, during early runs. A Fulflo Filter BR 10 3/4 Commercial Filter, Corporation, Melrose, Mass., was installed at the 30A pump discharge. This cleared the water satisfactorily.

Originally the test section was in a horizontal position to facilitate the photography. At low flow rates, one to two feet per second in the test section, nucleate boiling bubbles from the lower plate would rise and coalesce with the upper plate bubbles. It was feared that this might cause premature burnout on the upper plate,

[illegible]

The following letter was transmitted by Collins in a separate communication dated by a registered letter with 30 pounds attached to it. The letter was transmitted to the following address, which was given as a reference:

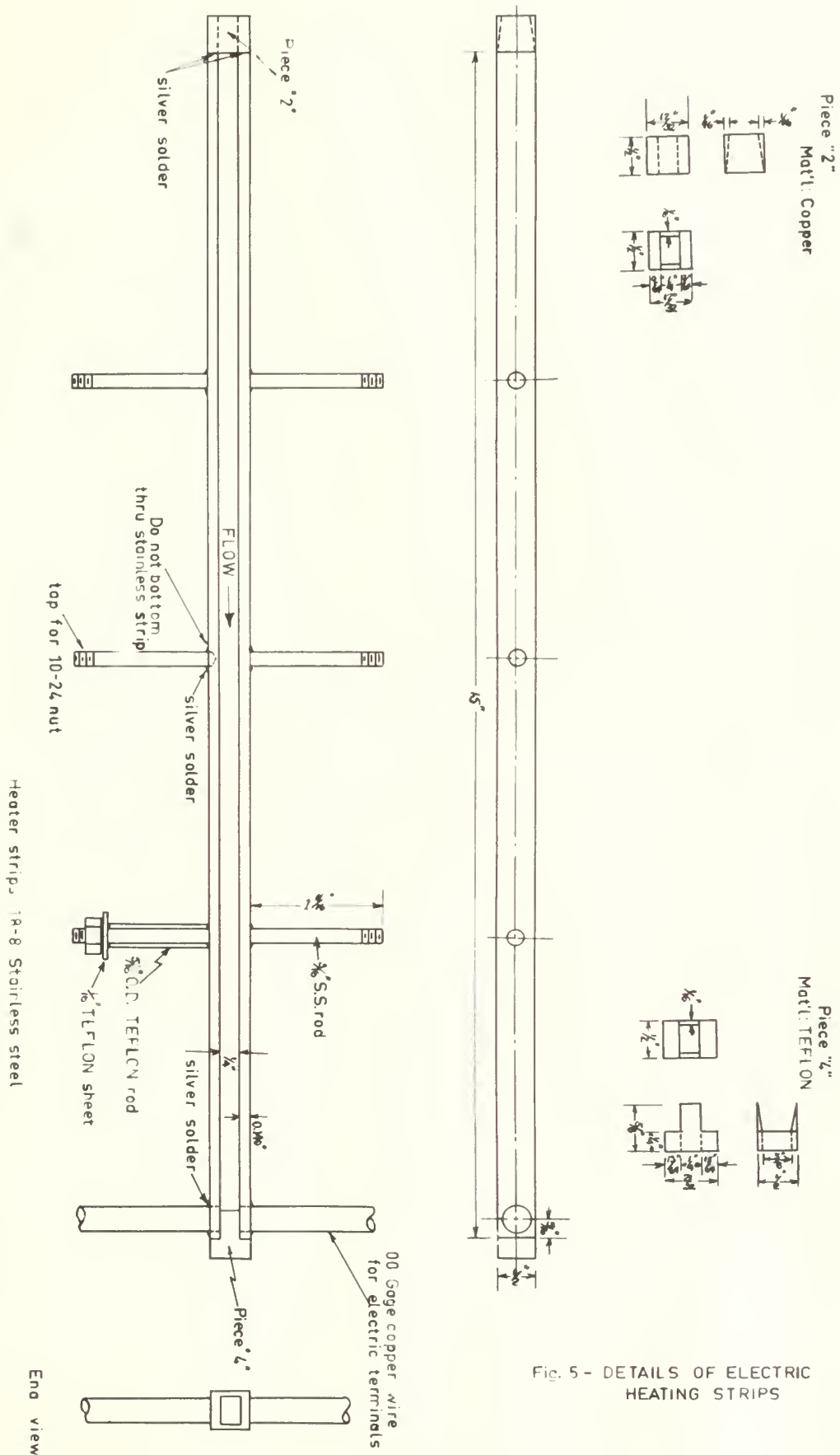


FIG. 5 - DETAILS OF ELECTRIC HEATING STRIPS

so the test section was mounted in a vertical position.

Fig. 5 "Details of Electric Heating Strips" shows the strips as used for the data runs. The first design did not have the six $3/16$ inch stainless steel rod supports for the heating strips, but only two small, $5/32$ inch, diameter, short, $1/4$ inch, stainless steel studs which fastened to a $5/16$ inch TEFLON dowel which in turn was tightened by a nut bearing against the outside of the main body of the test section frame. The small studs located at the midpoint of the strips proved inadequate to prevent compressive buckling of the heated strips during preliminary runs. The larger studs improved the situation, but did not eliminate the bowing of the strips completely. The silver solder on the backs of the strips and the thermal capacity of the larger studs undoubtedly caused variations in the electrical current density and the uniformity of the heat generation, but there was no apparent effect on the bubble boundary layer at the stud locations.

Fig. 5 Photograph of test section
(significantly)

as the test section was mounted in a vertical position.
Fig. 3 illustrates the method of mounting the test section.

The test section is used for the test runs. The test section
did not have the 1/2 inch stainless steel for

support for the test section, but only the small,
3/32 inch, stainless steel, 1/2 inch, stainless steel

which was mounted to a 1/2 inch stainless steel
in the test section by a nut passing through the test-

edge of the test body of the test section. The
small nut is located at the midpoint of the large power

inductor to prevent compressive buckling of the heated
large during test runs. The larger nut is located

the section, but did not eliminate the power of the
test completely. The silver solder on the back of the

silver and the thermal conductivity of the larger side
inductively caused variation in the electrical current

smallly and the uniformity of the test section. The
figure was an average of the test section, 1941

at the test section.

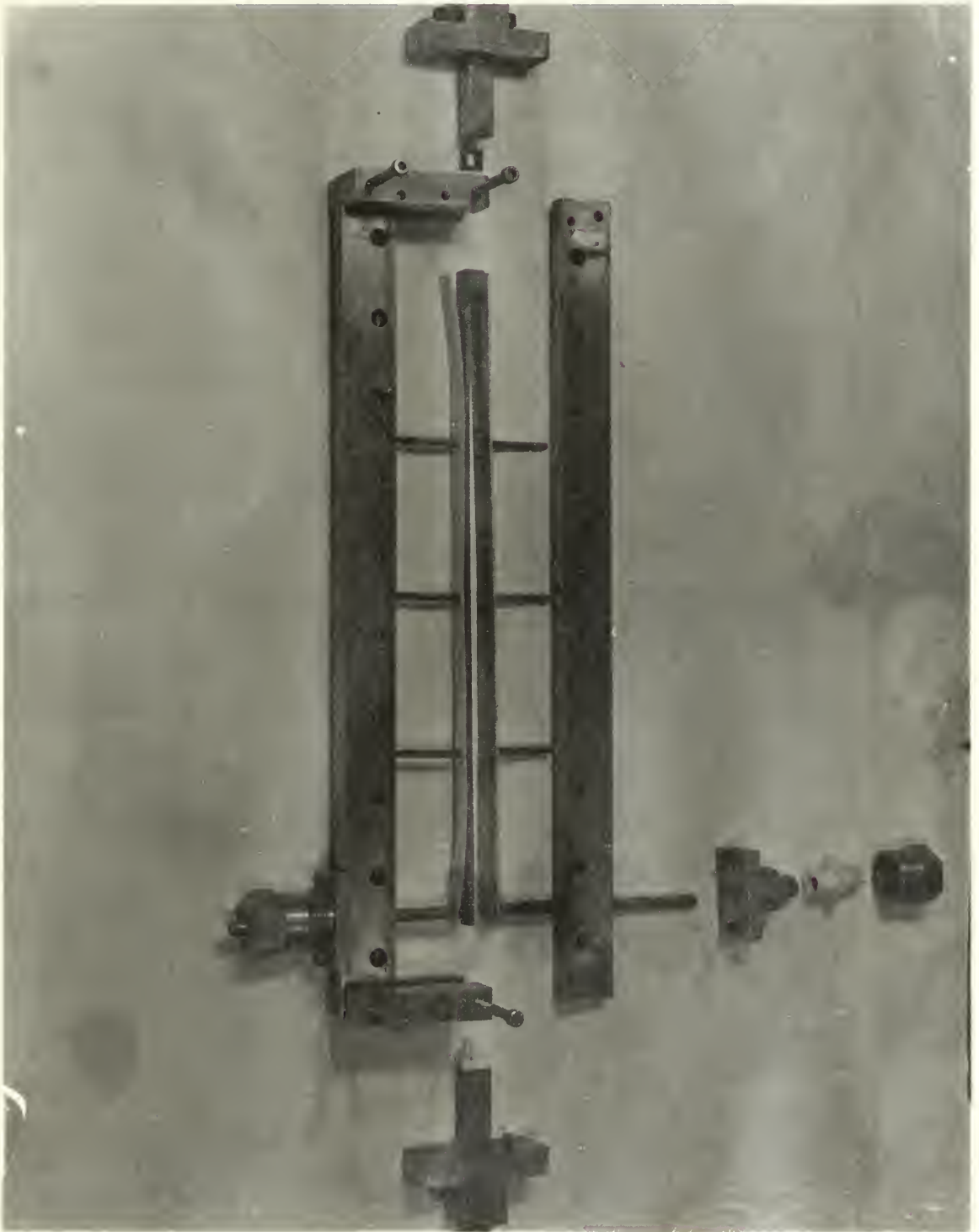


Fig.6 - Photograph of test section
(disassembled)

EXPERIMENTAL PROCEDURE

The distilled water used in the loop was taken from the degassifier where it had been boiled for one hour before each run. The electrical generator loading and the water flow velocity were set while the electrical preheaters were adjusted to maintain the desired water temperature at the test section inlet.

The voltage was measured across the test section electrical terminals with a Weston D.C. voltmeter, model 45, serial 2849, scale 0-1.5, 15, 150 volts. The ammeter on the motor generator control board gave the current readings. The boiling in the test section would cause appreciable increases in the system pressure. This necessitated readjustments in the flow as the pump characteristics were pressure sensitive. Conditions were allowed to stabilize by observing the test section outlet pressure. This pressure generally steadied within one minute. Photographs were taken with a Graphic View 4 inch x 5 inch still camera having Rapax lens, Wollensak Co., using Panatomic X film. Camera settings used were 1/25 sec and f 22. The test section was backlighted with a microflash light, type 1530-A, General Radio Co., Cambridge, Mass. The light was insufficient to light the entire test section at once, so each photograph covered a length of about eight inches. A typical sequence of photographs

For similar effect used in the loop was taken from the description which it has been before for the last before and from. The electrical generator loading and the other two velocity was not with the electrical generator was subjected to maintain the desired water temperature at the test section inlet.

Electrical equipment with a warning D.C. voltmeter, model 10-100, and a warning D.C. voltmeter, model 10-100.

translating. The rolling in the leaf section would cause
on the right translated section would have the section?

1. The first step is to identify the problem or goal. This involves understanding the current situation and what needs to be achieved.

necessary arrangements in the flow of the pump
 operation. The pump is a centrifugal type with
 a horizontal shaft and a vertical discharge pipe.

1. The proposed amendments are intended to clarify the language of the existing provisions of the Act and to bring the Act into conformity with the provisions of the Constitution of the United States.

one out of 100. The first condition was fulfilled with a
weight percentage of 1.11%. General relations used were 1/100

Fig 7- 47 ft/58

is appended as figs. 7, 8 and 9. All of the photographs and negatives are in the possession of Prof. J.A. Clark. Time was not available for the intended motion picture study.

Fig. 7- v 1 ft/sec
Q/A 83,000 Btu/hr ft²



Fig. 8 v 1 ft/sec
Q/A 166,000 Btu/hr ft²



Fig. 9 - v 1 ft/sec
Q/A 250,000 Btu/hr ft²



DISCUSSION OF RESULTS

An attempt was made to correlate the physical conditions in the channel such as heat flux density, flow velocity and fluid enthalpy, at the point where the two bubble boundary layers met or intermingled. This was not successful and it is believed that the principal difficulty was in establishing or defining the actual location of the junction. Before the vapor bubbles grow to a size which is about half of the channel width, the bubble is influencing the boundary layer on the opposite strip. With bubbles of this size, the photographs show that the flow is not symmetrical. A bubble deflects the water toward the opposite strip and seems to wipe off the bubbles or reduce the boundary layer thickness there.

The quantity h_x is the calculated bulk enthalpy at the point of intersection of the bubble boundary layers and is equal to the inlet enthalpy h_1 plus the energy added per pound by the heater strips between the inlet and the point

$$h_x = h_1 + 2 \left(\frac{Q}{A} \right) \frac{A_x}{w}$$

where A_x is the area of one strip between inlet and the point x , and w is mass flow rate through the channel. The experimental conditions for the various runs is tabulated on pages 25, 26, and 27. The following data was calculated for the runs indicated:

Picture		Picture	
7	-.062	14	-.031
8	-.064	15	-.034
9	-.027	16	-.035
10	-.030	17	-.040
11	-.053	18	-.056
12	-.043	19	-.039
13	-.031	20	-.048

The quantities h_f , the saturated liquid enthalpy, and h_{fg} , latent heat of evaporation correspond to the pressure measured at the test section outlet. No hydrostatic correction was made. It is significant that all of the points selected showed a negative "quality" or a bulk enthalpy less than the saturated enthalpy at the point where the vapor appears to be blocking the channel.

It must be remembered, however, that the bubbles are actually three dimensional rather than two as is implied here when the point of intersection is assumed. The actual "quality" is undoubtedly less than the value calculated since all the energy generated in the strips was assumed to be transferred to the fluid. There were certainly heat losses through the back of the heating strips both by conduction and by boiling of water which leaked on to the back of the strip. No theoretical calculations were made to estimate the magnitude of this loss nor was a heat balance attempted

on the section because of inadequate instrumentation. It is believed that the losses are less than ten percent.

Several "exploratory" runs were made in an effort to achieve a higher quality at the test section outlet. No photographs were taken. With $Q/A = 455,000 \text{ Btu/hr ft}^2$, $v = 1 \text{ ft/sec}$, $t_1 = 170^\circ$ and $p = 45 \text{ psia}$, the calculated quality at outlet was about $\sim 1.4\%$. The last few inches of the channel appeared to be almost all vapor.

$Q/A = 450,000 \text{ Btu/hr ft}^2$, $v = 0.8 \text{ ft/sec}$, $t_1 = 184$ and $p = 53 \text{ psia}$ gave a pulsating flow with slugs of vapor surging up the channel. The calculated outlet quality was $\sim 4.7\%$. The highest quality achieved was $\sim 14.4\%$ with $Q/A = 440,000 \text{ Btu/hr ft}^2$, $v = 0.5 \text{ ft/sec}$, $t_1 = 196^\circ$ and $p = 60 \text{ psia}$. With these conditions the upper two thirds of the test section was mostly vapor with violent boiling in the bottom third.

Plots were made of δ , the thickness or height of the bubble boundary layer, against a parameter H , which expressed the subcooling of the bulk liquid at the location where was measured. H is the same negative "quality" or subcooling spoken of previously.

$$H \equiv \frac{h_s - h_f}{h_{fg}}$$

where

$$h_s = h_i + 2 \left(\frac{Q}{A} \right) \frac{A_s}{w}$$

and h_δ is the calculated enthalpy at the point where δ was measured. The value of H was also calculated ignoring all heat losses. As H is a calculated quantity, the experimental uncertainty is of interest. With the following experimental variations:

flow velocity ± 0.1 ft/sec for $v = 1$ ft/sec

pressure ± 0.5 psia

inlet temperature $\pm 0.5^\circ\text{F}$

generator current ± 5.0 amps

the resulting uncertainty in H can be estimated. Taking run #29, which is Fig. 8, as an example where $\delta = .083$ inches at a distance $x = 9.35$ inches from the beginning of the heated strip.

$$Q = 8.3 \text{ volts} \times 600 \pm 5 \text{ amps} = 4.72 \pm 0.4 \text{ Btu/sec}$$

$$w = .11 \pm .01 \text{ lb/sec}$$

$$h_\delta = h_1 + Q \cdot \frac{1}{w} \left(\frac{x}{L} \right) \quad L = 14.7'' \text{ length of heated strip}$$

$$\text{with } t_1 = 200^\circ\text{F} \pm 0.5^\circ\text{F}, h_1 = 168.0 \pm 0.5 \text{ Btu/lb}$$

$$\text{since } p = 41 \pm 0.5 \text{ psia}$$

$$h_f = 237.5 \pm 0.7 \text{ Btu/lb}$$

$$h_{fg} = 932.6 \pm 0.5 \text{ Btu/lb}$$

$$H = \frac{h_\delta - h_f}{h_{fg}}$$

2

3

and is the standard deviation of the first series
was calculated. The value of σ was also calculated assuming
all first series. As it is a calculated quantity, the
approximate accuracy is at least 1% with the
following approximate calculation:

$$\text{True velocity} \pm 0.1 \text{ km/sec for } v = 1 \text{ km/sec}$$

$$\pm 0.5 \text{ km/sec}$$

$$\text{True temperature} \pm 0.5^\circ\text{C}$$

$$\text{True density} \pm 0.5 \text{ g/cm}^3$$

The resulting uncertainty in σ is estimated. From

$$\text{for } \sigma = 1 \text{ km/sec, } \sigma = 0.1 \text{ km/sec, } \sigma = 0.01 \text{ km/sec}$$

$$\text{the resulting uncertainty in } \sigma = 0.1 \text{ km/sec, } \sigma = 0.01 \text{ km/sec}$$

it can be seen that

$$\sigma = 0.1 \text{ km/sec, } \sigma = 0.01 \text{ km/sec, } \sigma = 0.001 \text{ km/sec}$$

$$\sigma = 0.1 \text{ km/sec, } \sigma = 0.01 \text{ km/sec, } \sigma = 0.001 \text{ km/sec}$$

where σ is the standard deviation of the first series

$$\sigma = \sigma_1 + \sigma_2 \left(\frac{x}{L} \right)$$

$$\text{with } \sigma_1 = 0.001 \text{ km/sec, } \sigma_2 = 0.001 \text{ km/sec, } \sigma_3 = 0.001 \text{ km/sec}$$

$$\text{since } \sigma = 0.1 \text{ km/sec, } \sigma = 0.01 \text{ km/sec, } \sigma = 0.001 \text{ km/sec}$$

$$\sigma = 0.1 \text{ km/sec, } \sigma = 0.01 \text{ km/sec, } \sigma = 0.001 \text{ km/sec}$$

$$\sigma = 0.1 \text{ km/sec, } \sigma = 0.01 \text{ km/sec, } \sigma = 0.001 \text{ km/sec}$$

$$\sigma = \frac{\sigma_1 - \sigma_2}{\sigma_1 + \sigma_2}$$

$$H = \frac{(195.3 \pm 3.3) - (237.5 \pm 0.7)}{932.6 \pm 0.5}$$

$$H = 0.045 \pm .003$$

This shows an uncertainty of about 6% in H . The largest variations were in the water velocity and the generator current measurements, consequently the scatter was appreciably greater for the low flow and low power runs. This is quite possibly the explanation for the seeming inconsistencies shown on Fig. 10 where $Q/A = 83,000$ Btu/hr ft² and the 3 ft/sec is to the right of the 2 ft/sec run.

The plots of δ vs H show that the growth of the bubble boundary layer is as would be expected. It is less for the greater subcooling and higher velocities while greater for the higher heat flux densities. These variations are given quantitatively by the graphs. Since the general shape of the various curves is similar, it was thought that a correlation for the nucleation points (i.e.

$\delta = 0$) might be found. As the pressure was different for the various runs, a pressure parameter for nucleation was sought. Using the liquid superheat at incipient nucleation, a term was added to the "subcooling" parameter H used previously. If

$$(t_w^* - t_f) = f(p)$$

where t_w^* is the wall temperature at the point of nucleation and t_f is the bulk fluid temperature.

$$h_w^* - h_g = f(p)$$

If p is assumed constant then h_f and h_{fg} are constant,

$$\frac{(h_w - h_f)^* + (h_f - h_g)}{h_{fg}} = \frac{h_w^* - h_g^*}{h_{fg}}$$

$$M \equiv \left(\frac{h_w - h_f}{h_{fg}} \right) - H \quad \text{where} \quad H = \frac{h_g^* - h_f}{h_{fg}}$$

Values for $t_w^* - t_f$ as a function of pressure were taken from Figure IV-C-2 "Maximum Experimental and Theoretical Degree of Liquid Superheat" from ref. (3).

The experimental superheat curve for the stainless steel - water system was used. The pressure nucleation correction was applied to smoothed curves of δ vs M . The resulting correlation is shown in Fig. 21. While it is true that this resulted in a closer grouping of the data, such a high value of superheat ($\sim 150^\circ\text{F}$) obtained in an experiment where the water was very clean, unheated and static is unlikely in a moving fluid being heated. It is felt that a superheat of about thirty degrees would be more reasonable. Any such lower value of superheat would tend to scatter the curves more. It is apparent that a generalized correlation is yet to be gained.

LIST OF SYMBOLS

A_{δ}	area of heater strip from inlet to point where δ was measured	(sq. in.)
A_x	area of heater strip from inlet to point where $\delta = 1/2 y$	(sq. in.)
	height of bubble boundary layer	(in)
h_{δ}	fluid enthalpy at point where δ is measured	(Btu/lb)
h_f	enthalpy of liquid	(Btu/lb)
h_{fg}	latent heat of evaporation	(Btu/lb)
h_i	fluid enthalpy at test section inlet	(Btu/lb)
h_x	fluid enthalpy at point x	(Btu/lb)
H	"subcooling" parameter $\equiv \frac{h_{\delta} - h_f}{h_{fg}}$	
L	length of heated strip	14.7"
M	"nucleation - subcooling" parameter $\equiv \frac{(h_w - h_f^*) - (h_{\delta}^* - h_f)}{h_{fg}}$	
p	test section outlet pressure	(psia)
Q/A	heat flux density	(Btu/hr ft ²)
t_w	temperature of heated wall	(°F)
t_f	temperature of fluid	(°F)
v	flow velocity	(ft/sec)
w	mass flow rate	(lb/sec)
x	distance from inlet where δ is measured	(in)
y	spacing between heater strips	(in)
*	indicates conditions at bubble nucleation	

1	Fluid analysis at point 1	(10/10)
2	Fluid analysis at point 2	(10/10)
3	Fluid analysis at point 3	(10/10)
4	Fluid analysis at point 4	(10/10)
5	Fluid analysis at point 5	(10/10)
6	Fluid analysis at point 6	(10/10)
7	Fluid analysis at point 7	(10/10)
8	Fluid analysis at point 8	(10/10)
9	Fluid analysis at point 9	(10/10)
10	Fluid analysis at point 10	(10/10)

24-21

$$\frac{(2N - 8N) - (2N - 6N)}{2N} = \frac{-6N + 6N}{2N} = \frac{0}{2N} = 0$$

1. distance from inlet to nozzle (in)
2. distance from inlet to nozzle (in)
3. mass flow rate (lb/sec)
4. flow velocity (ft/sec)
5. temperature of fluid (°F)
6. density of fluid (lb/ft³)
7. loss coefficient (K)

Experimental and Calculated Data on the Bubble Boundary Layer

Elect. Volts	amps	i/A	v ft/sec	t_1 OF	P psia	δ in.	x in.	-H	Elect. Volts	amps	i/A	v ft/sec	t_1 OF	P psia	δ in.	x in.	-H
#1 4.5	330	49,000	1	180	15	.00 .04 .081 .081	2.11 7.85 9.27 10.96	.029 .026 .025 .022	#9 8.3	605	160,000	3	180	17	.00 .092 .10 .125 .083 .117	2.87 8.26 9.53 10.87 11.75 12.71	.038 .033 .031 .030 .029 .028
#2 5.9	430	83,000	1	180	17	.00 .016 .032 .089 .113	4.26 5.78 8.30 9.11 10.71	.035 .032 .027 .025	#10 10.3	730	250,000	3	180	20	.00 .043 .078 .086 .104 .12	2.75 8.27 9.47 9.71 10.85 12.55	.046 .038 .036 .036 .034 .031
#3 7.8	505	147,000	1	180	28	.00 .04 .056 .072 .113	2.75 3.59 8.49 8.15 10.23	.007 .004 .050 .052 .046	#11 12.3	850	333,000	2	180	30	.00 .117 .109 .107 .117	1.87 8.45 9.71 10.62 11.57	.083 .070 .067 .065 .063
#5 8.4	605	166,000	2	180	22	.00 .024 .032 .064 .072	2.75 4.27 5.89 8.05 10.01	.050 .047 .044 .041 .038	#12 12.3	850	333,000	3	180	26	.00 .000 .083 .108 .117	2.25 7.06 8.34 9.59 10.33	.061 .050 .049 .046 .045
#6 10.3	730	250,000	2	180	20	.00 .034 .034 .052 .06	2.25 3.01 4.84 7.0 9.15	.001 .059 .055 .050 .045 .041	#13 12.3	850	333,000	4	180	20	.00 .042 .000 .083 .10	2.75 7.85 9.0 9.66 10.96	.046 .038 .036 .036 .034
#7 12.5	920	416,000	2	180	48	.00 .075 .09 .11	1.75 8.16 9.05 10.41	.100 .075 .070 .066	#14 12.3	850	333,000	5	174	17	.00 .041 .066 .066	3.0 7.75 8.84 9.75	.040 .040 .039 .038
#8 15.0	1,000	500,000	2	180	50	.00 .082 .108 .125	1.75 7.75 8.75 9.06	.111 .082 .078 .076	#15 12.2	855	333,000	5	180	19	.00 .069 .078 .112 .129	2.87 8.94 9.99 11.51 13.42	.047 .037 .035 .034 .031

Experimental and Calculated Data on the Bubble Boundary Layer

Fict. Volts	Amps μ/A	v ft/sec	t_1 of	p psia	δ in.	x in.	-h	Fict. Volts	amps μ/A	v ft/sec	t_1 of	p psia	δ in.	x in.	-h
#16 13.5	930 410,000	5	180	22	.06	3.0	.049	#25 5.8	435 83,000	3	200	20	.06	4.37	.020
					.067	8.0	.042						.060	0.45	.027
					.058	8.5	.041						.060	0.87	.020
					.075	8.84	.040						.033	7.50	.025
					.075	9.82	.039						.067	8.04	.025
					.075	10.02	.038						.067	8.71	.025
					.067	11.8	.030						.083	9.0	.025
					.084	12.0	.034						.075	9.75	.024
#17 13.4	925 410,000	4	180	24	.06	2.37	.058						.117	10.42	.024
					.042	8.29	.046						.108	11.07	.023
					.10	8.53	.046						.108	12.84	.023
					.17	9.03	.045	#26 8.3	000 100,000	4	200	21	.06	4.12	.032
					.083	9.40	.044						.05	8.93	.027
					.092	9.87	.043						.033	9.20	.027
					.133	10.29	.042						.067	9.90	.027
					.10	11.21	.040						.108	10.07	.020
					.133	11.82	.039						.10	11.12	.020
#18 13.5	925 410,000	3	180	32	.06	1.87	.076						.075	12.04	.025
					.084	7.99	.058						.108	13.02	.024
					.108	8.71	.050						.10	14.12	.024
					.125	9.28	.055	#27 8.3	000 100,000	3	200	23	.06	2.75	.037
#20 14.5	990 476,000	4	180	29	.06	2.0	.068						.060	7.84	.032
					.058	8.09	.055						.075	8.33	.031
					.067	8.75	.054						.058	9.03	.030
					.117	9.3	.052						.067	9.35	.030
					.092	10.0	.051						.083	9.92	.029
					.092	11.3	.048						.075	10.91	.028
					.108	12.0	.046						.15	11.04	.028
#22 5.9	430 83,000	1	200	25	.06	2.75	.038	#28 8.3	000 100,000	2	200	27	.06	2.37	.049
					.067	6.01	.030						.067	7.95	.040
					.075	7.05	.028						.075	8.21	.040
					.091	7.75	.027						.117	8.41	.040
					.108	11.0	.025						.083	9.17	.036
					.101	12.09	.023						.108	9.87	.037
#24 5.9	430 83,000	2	200	20	.06	2.12	.027	#29 8.3	000 100,000	1	200	41	.06	2.0	.068
					.067	7.07	.023						.054	7.70	.050
					.067	8.14	.023						.075	8.17	.049
					.10	8.07	.023						.058	8.53	.048
					.067	8.87	.023						.10	8.75	.047
					.067	9.37	.022						.083	9.35	.045
					.05	9.02	.022						.10	9.75	.041
					.075	9.70	.022						.125	10.35	.042
					.083	10.28	.021						.12	11.90	.037
					.083	10.43	.021	#30 10.5	725 250,000	4	200	50	.06	2.5	.070
					.075	12.82	.019						.084	8.25	.058
					.094	14.22	.018						.10	9.41	.054
					.10	14.62	.018						.108	9.75	.054
					.10	14.62	.018						.117	10.35	.042

Calculated Values of the "Nucleation and Subcooling"
Parameter M for smoothed curves of δ

Fict.	δ	$(t_w - t_f)^*$	M	Fict.	δ	$(t_w - t_f)^*$	M
#2	0	160	.200	#16	0	150	.206
	.05		.193		.05		.197
	.10		.191		.10		.194
#3	0	142	.215	#17	0	147	.212
	.05		.206		.05		.201
	.10		.198		.10		.197
#6	0	144	.197	#18	0	136	.220
	.05		.188		.05		.206
	.10		.184		.10		.200
#7	0	120	.229	#20	0	140	.216
	.05		.204		.05		.202
	.10		.198		.10		.198
#8	0	114	.235	#22	0	145	.190
	.05		.212		.05		.183
	.10		.203		.10		.178
#9	0	160	.203	#24	0	154	.187
	.05		.198		.05		.184
	.10		.193		.10		.182
#10	0	154	.222	#25	0	154	.187
	.05		.208		.05		.184
	.10		.203		.10		.184
#11	0	131	.223	#26	0	152	.189
	.05		.211		.05		.185
	.10		.208		.10		.183
#12	0	144	.212	#27	0	148	.192
	.05		.203		.05		.1855
	.10		.198		.10		.183
#13	0	154	.206	#28	0	142	.199
	.05		.198		.05		.191
	.10		.194		.10		.1855
#15	0	156	.216	#29	0	126	.203
	.05		.208		.05		.184
	.10		.204		.10		.179
				#30	0	114	.214
					.05		.185
					.10		.178

GRAPHIC PLOTS OF DATA

The following figures are arranged first for constant heat flux density Q/A with varying flow velocities to show the velocity effect on the growth of the bubble boundary layer for different subcoolings. The data was next cross-plotted at a constant flow velocity to show the effect of changing heat flux density against subcooling.



REPORT OF THE

The following figures are arranged in order of increasing
 heat flux density & with varying line velocities in some
 the velocity effect on the amount of the source is
 taken for different substances. The data are given in
 figures as a general idea of the effect of
 chemical and the source of the substance.

Fig. 10 - $q/A = 83,000 \text{ Btu/hr ft}^2$

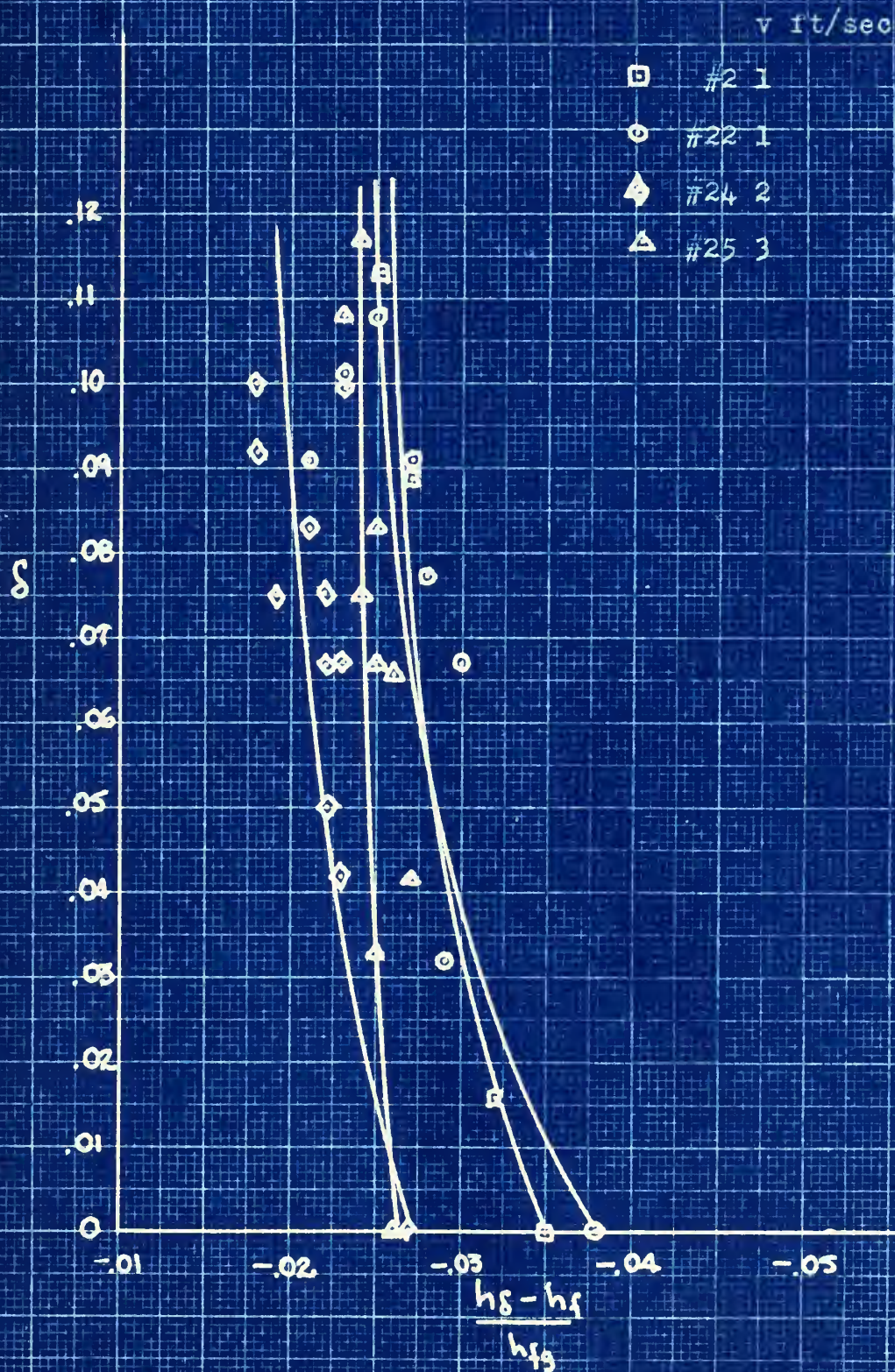


Fig. 11 - $Q/A = 166,000 \text{ Btu/hr ft}^2$

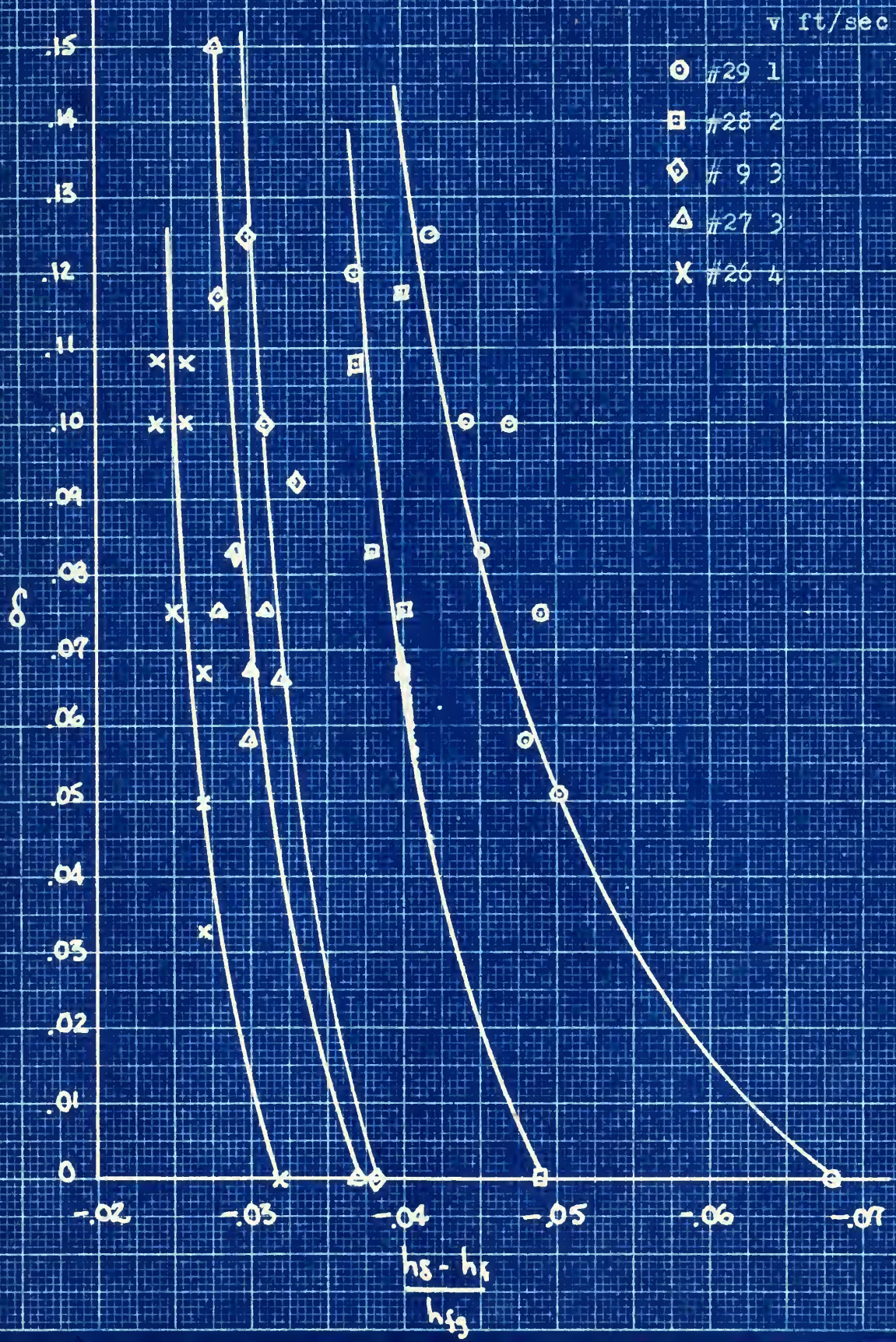


Fig. 12 - $q/r = 250,000$ Btu/hr ft²

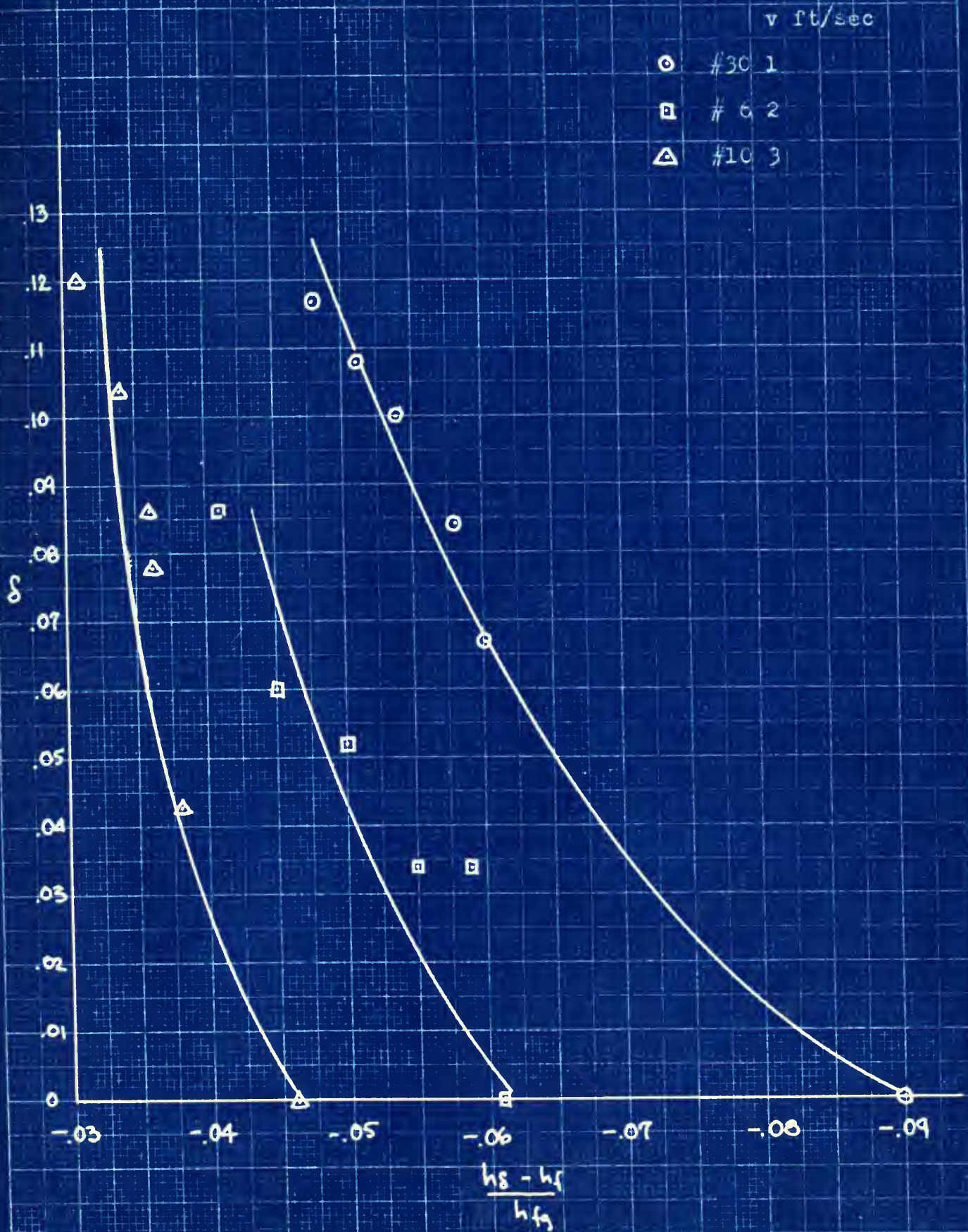


Fig. 13 - $Q/A = 333,000 \text{ Btu/hr ft}^2$

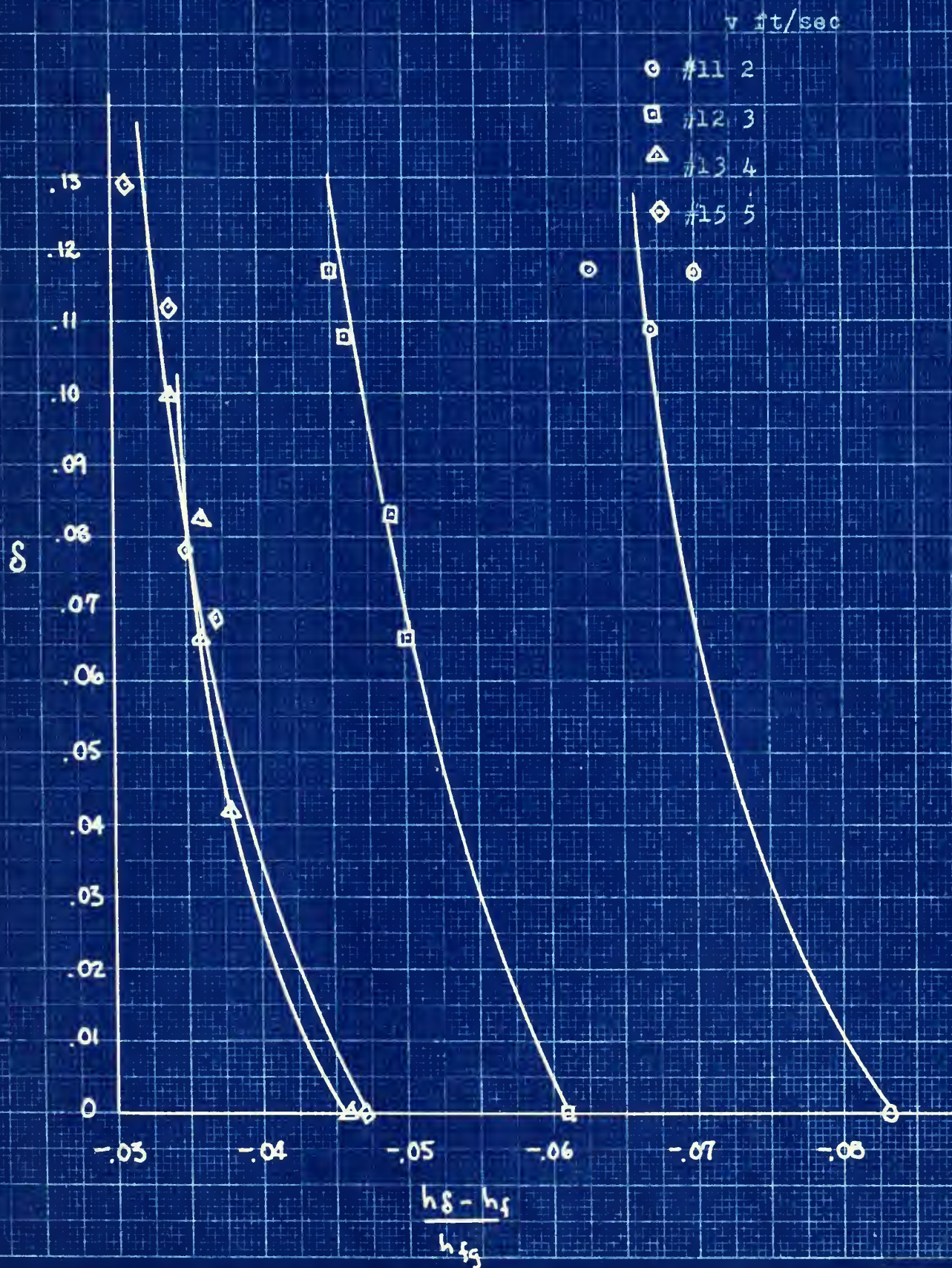


Fig. 14 - $Q/A = 416,000 \text{ Btu/hr ft}^2$

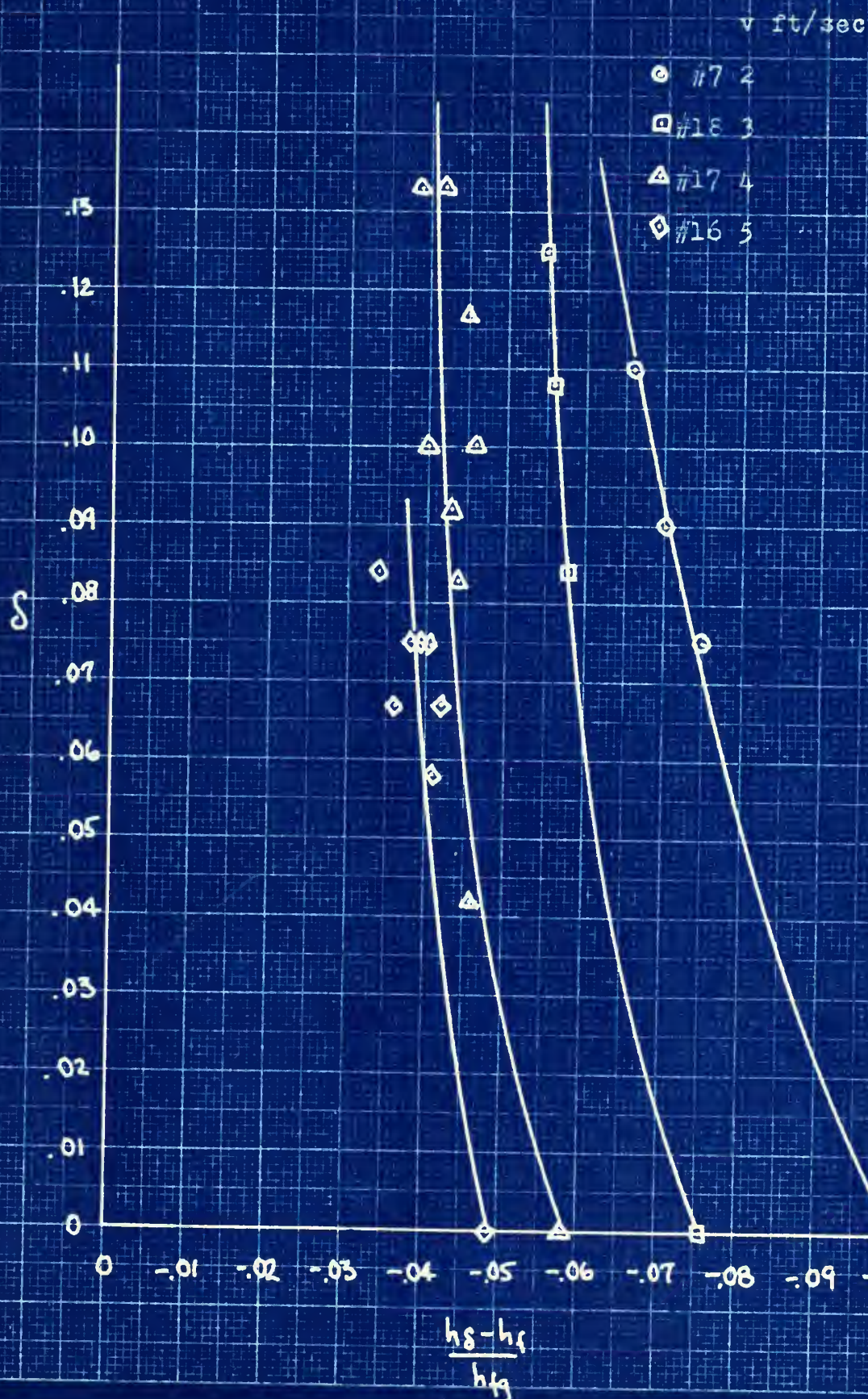


Fig. 15 - $Q/A = 475,000 \text{ Btu/hr ft}^2$

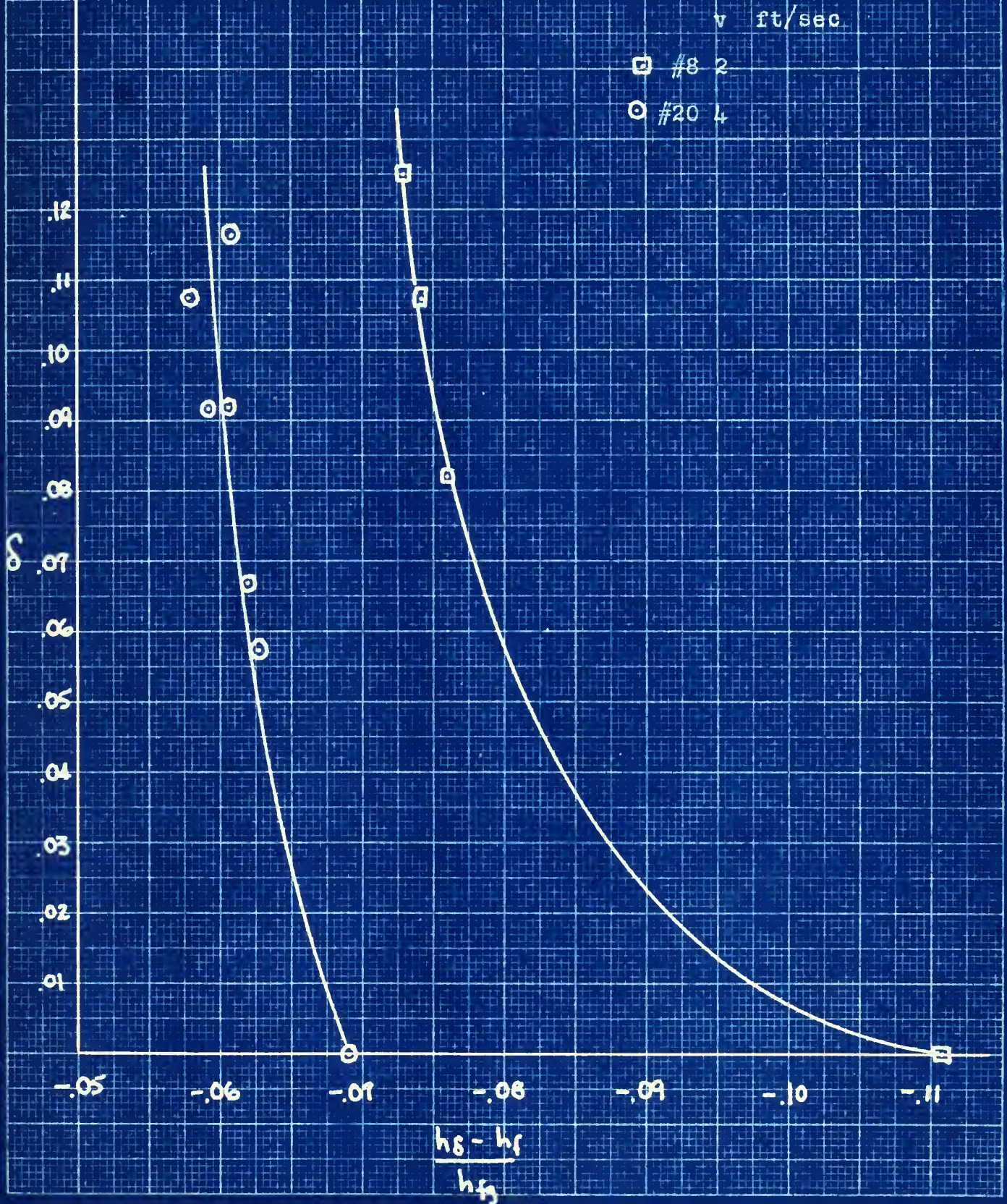


Fig. 16 - $V = 1 \text{ ft/sec.}$

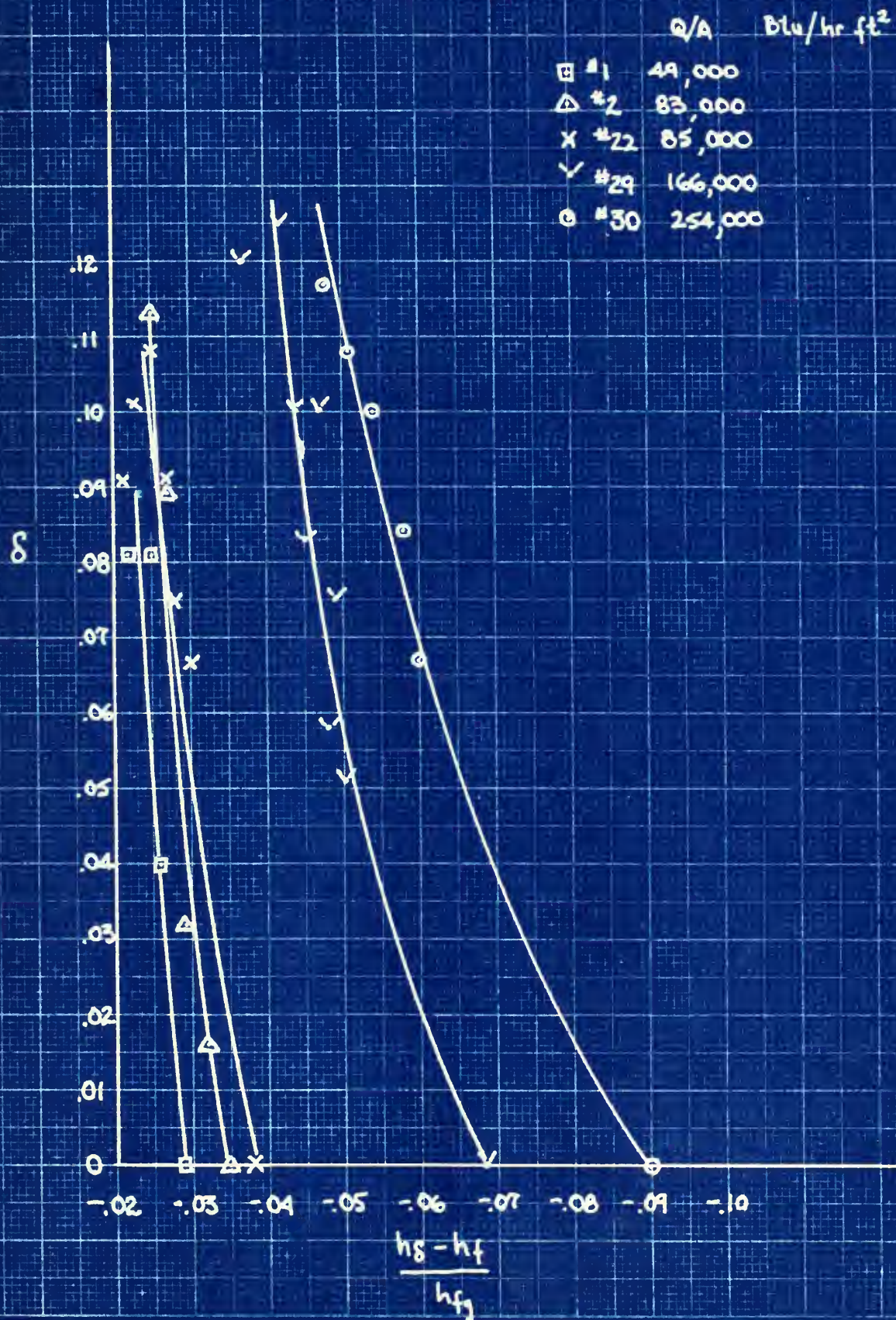


Fig. 17 - $v = 2$ ft/sec

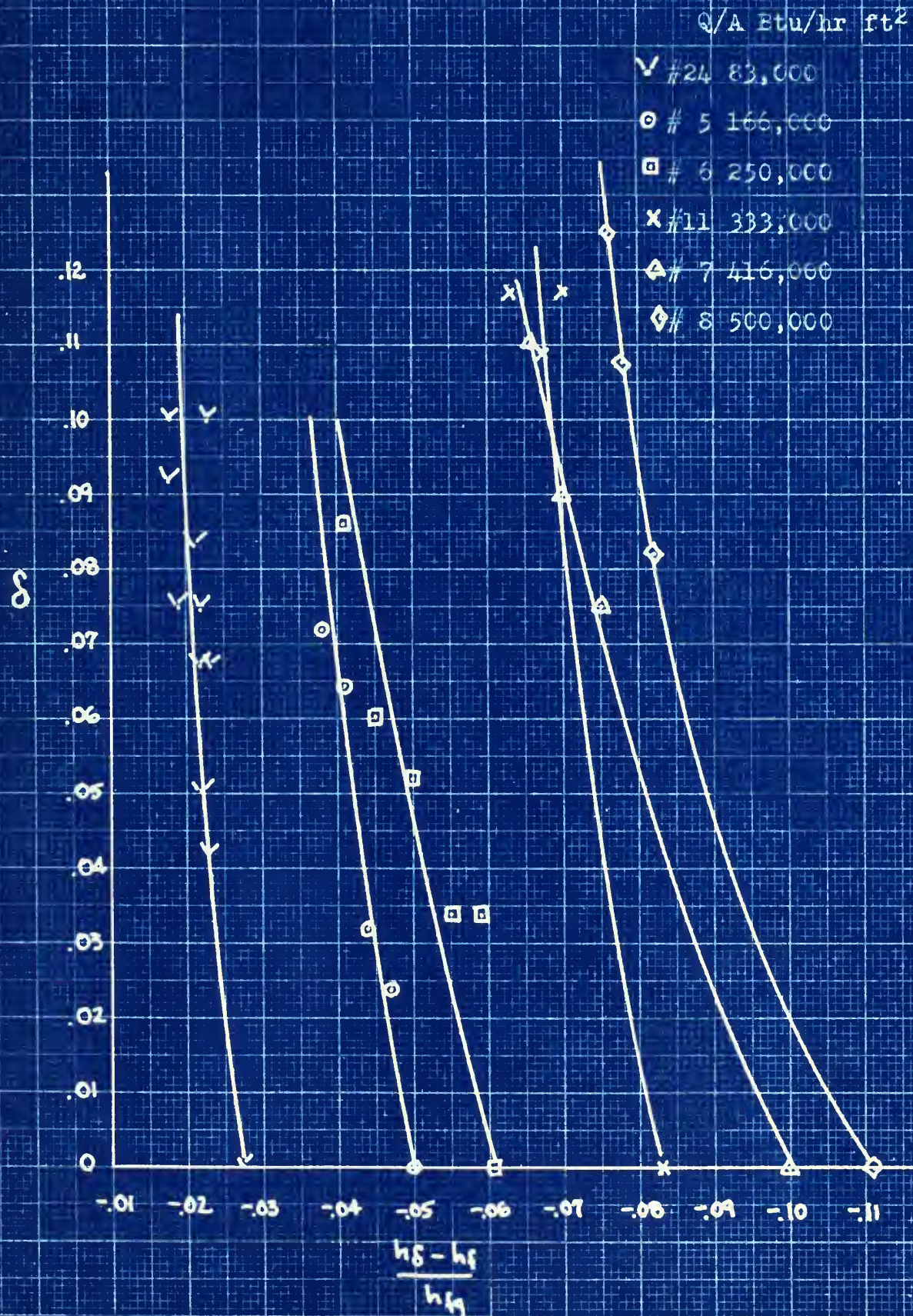


Fig. 18 - $v = 3$ ft/sec

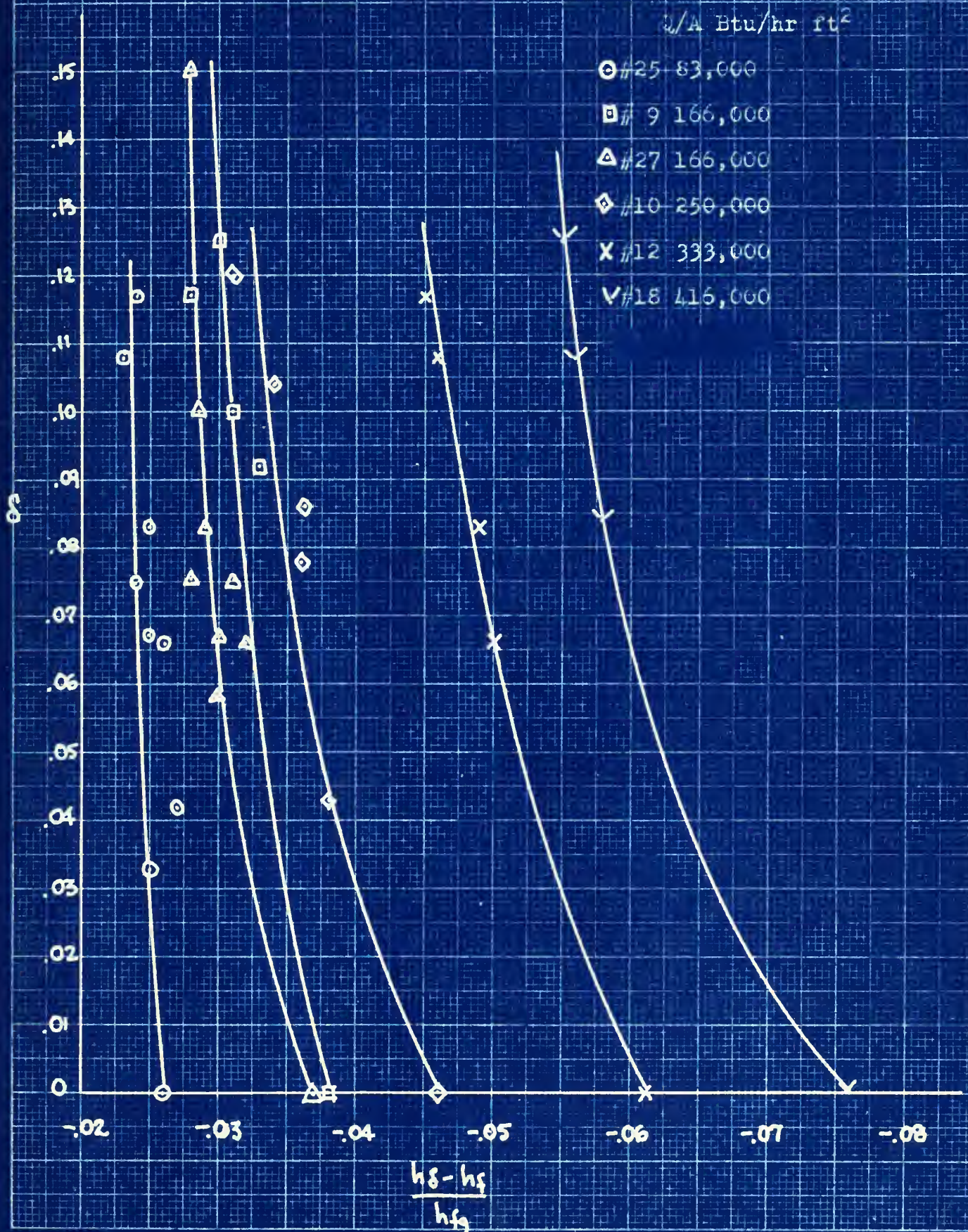


Fig. 19 - $v = 4$ ft/sec

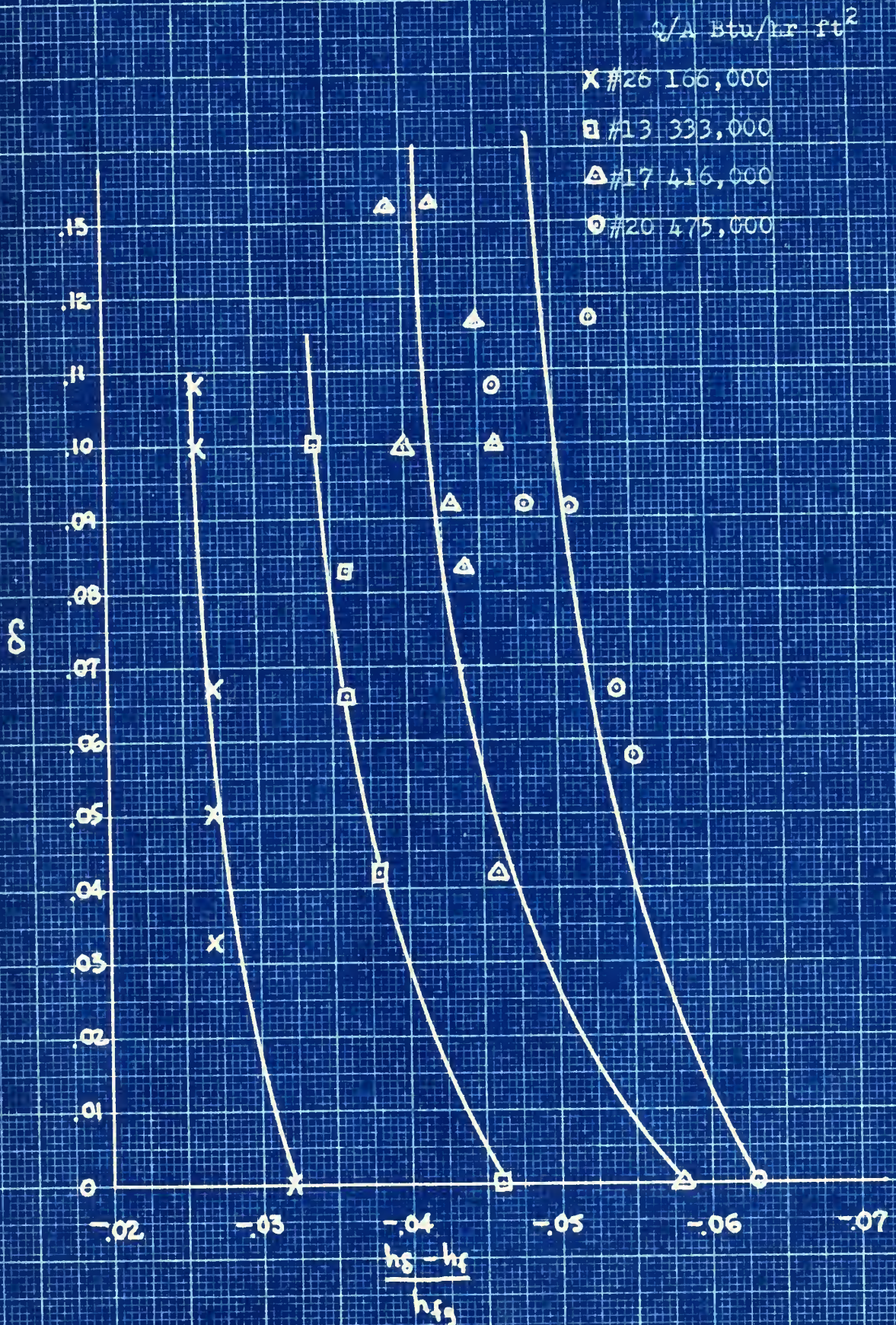


Fig. 20 - $v = 5$ ft/sec

Q/A Btu/hr ft²

○ #15 333,000

□ #16 416,000

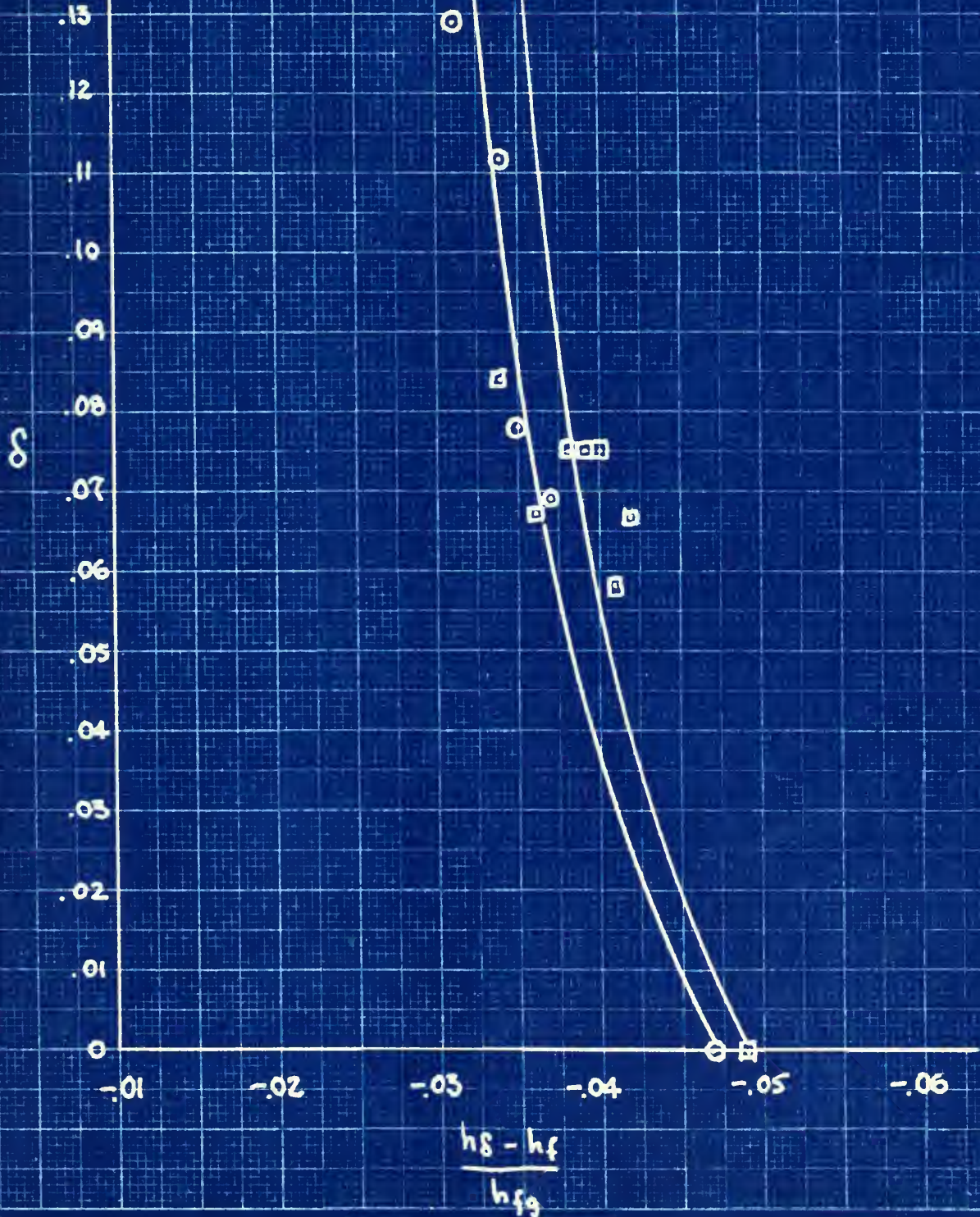
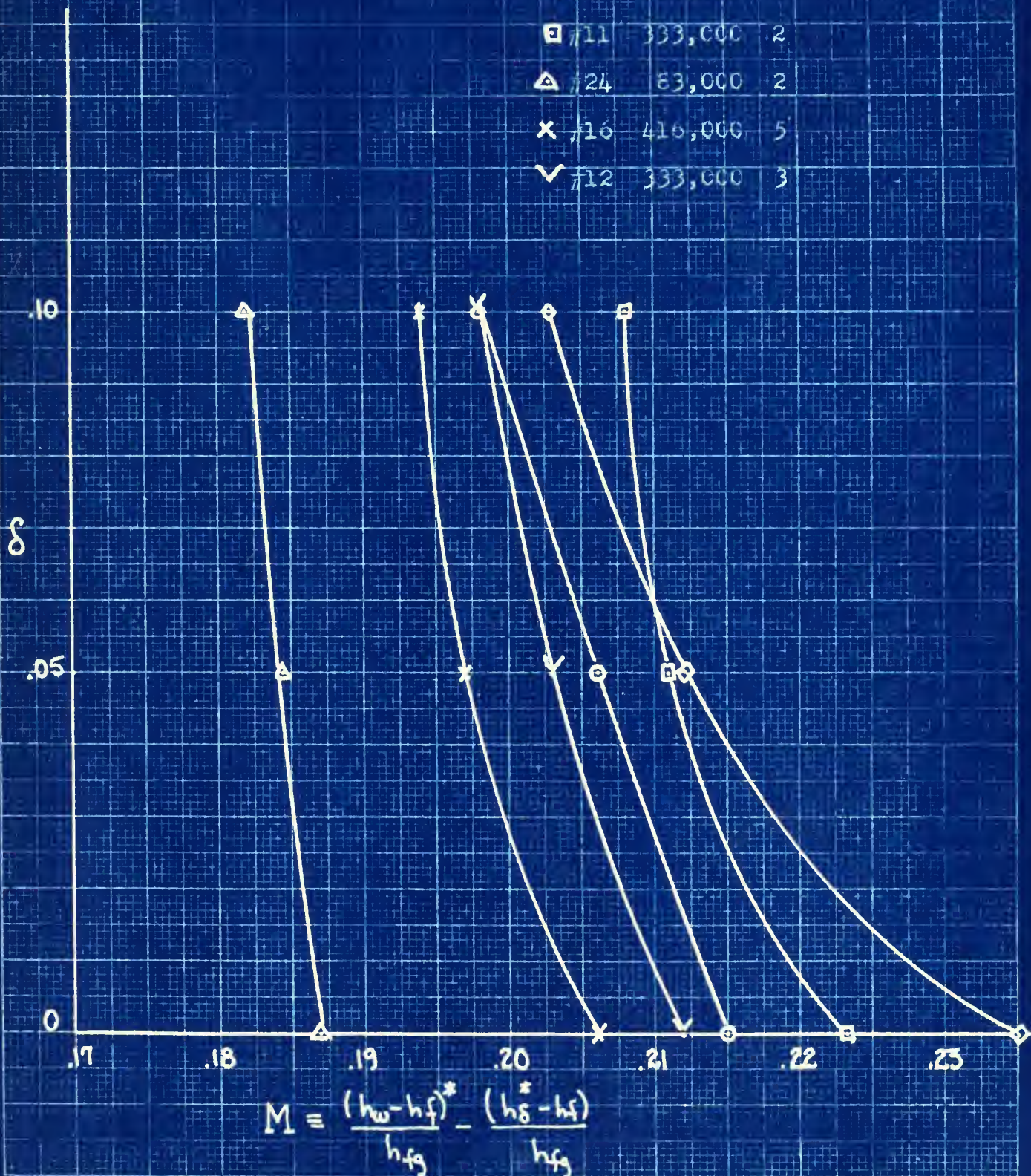


Fig. 21

		Q/A	v
○	#3	147,000	1
◇	#8	500,000	2
□	#11	333,000	2
△	#24	83,000	2
×	#16	416,000	5
▽	#12	333,000	3



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